

## Important Algebraic Formulas

$$(a + b)^2 = a^2 + b^2 + 2ab$$

$$(a - b)^2 = a^2 + b^2 - 2ab$$

$$a^2 - b^2 = (a + b)(a - b)$$

$$a^2 + b^2 = (a + b)^2 - 2ab \quad \text{or} \quad a^2 + b^2 = (a - b)^2 + 2ab$$

$$a^3 + b^3 = (a + b)(a^2 - ab + b^2) = (a + b)^3 - 3ab(a + b)$$

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2) = (a - b)^3 + 3ab(a - b)$$

$$2(a^2 + b^2) = (a + b)^2 + (a - b)^2$$

$$(a + b)^2 - (a - b)^2 = 4ab$$

$$a^4 + b^4 = (a + b)(a - b)[(a + b)^2 - 2ab]$$

$$(a - b)^2 = (a + b)^2 - 4ab$$

$$(a + b)^2 = (a - b)^2 + 4ab$$

$$a^4 + b^4 = [(a + b)^2 - 2ab]^2 - 2(ab)^2$$

$$(a + b + c)^2 = a^2 + b^2 + c^2 + 2ab + 2bc + 2ca$$

$$(a + b - c)^2 = a^2 + b^2 + c^2 + 2ab - 2bc - 2ca$$

$$(a - b - c)^2 = a^2 + b^2 + c^2 - 2ab + 2bc - 2ca$$

$$a^3 + b^3 + c^3 - 3abc = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$$

$$a^4 + a^2b^2 + b^4 = (a^2 + ab + b^2)(a^2 - ab + b^2)$$

$$a^4 + a^2 + 1 = (a^2 + a + 1)(a^2 - a + 1)$$

$$\text{if } a + b + c = 0 \text{ then } a^3 + b^3 + c^3 = 3abc$$

$$a^8 - b^8 = (a^4 + b^4)(a^2 + b^2)(a + b)(a - b)$$

Regra	Exemplo
$a^m \times a^n = a^{m+n}$	$2^5 \times 2^3 = 2^8$
$a^m \div a^n = a^{m-n}$	$5^7 \div 5^3 = 5^4$
$(a^m)^n = a^{m \times n}$	$(10^3)^7 = 10^{21}$
$a^1 = a$	$17^1 = 17$
$a^0 = 1$	$34^0 = 1$
$\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}$	$\left(\frac{5}{6}\right)^2 = \frac{25}{36}$
$a^{-m} = \frac{1}{a^m}$	$9^{-2} = \frac{1}{81}$
$a^{\frac{x}{y}} = \sqrt[y]{a^x}$	$49^{\frac{1}{2}} = \sqrt[2]{49} = 7$

### Powers and Square Roots To Memorize!!!

$1^2 = 1$	$1^3 = 1$	$\sqrt{1} = 1$
$2^2 = 4$	$2^3 = 8$	$\sqrt{4} = 2$
$3^2 = 9$	$3^3 = 27$	$\sqrt{9} = 3$
$4^2 = 16$	$4^3 = 64$	$\sqrt{16} = 4$
$5^2 = 25$	$5^3 = 125$	$\sqrt{25} = 5$
$6^2 = 36$	$6^3 = 216$	$\sqrt{36} = 6$
$7^2 = 49$	$1^4 = 1$	$\sqrt{49} = 7$
$8^2 = 64$	$2^4 = 16$	$\sqrt{64} = 8$
$9^2 = 81$	$3^4 = 81$	$\sqrt{81} = 9$
$10^2 = 100$	$4^4 = 256$	$\sqrt{100} = 10$
$11^2 = 121$	$5^4 = 625$	$\sqrt{121} = 11$
$12^2 = 144$	$1^5 = 1$	$\sqrt{144} = 12$
$13^2 = 169$	$2^5 = 32$	$\sqrt{169} = 13$
$14^2 = 196$	$3^5 = 243$	$\sqrt{196} = 14$
$15^2 = 225$	$4^5 = 1024$	$\sqrt{225} = 15$
$16^2 = 256$	$1^6 = 1$	$\sqrt{256} = 16$
$17^2 = 289$	$2^6 = 64$	$\sqrt{289} = 17$
$18^2 = 324$	$3^6 = 729$	$\sqrt{324} = 18$
$19^2 = 361$	$1^7 = 1$	$\sqrt{361} = 19$

## Square and Square Root Table

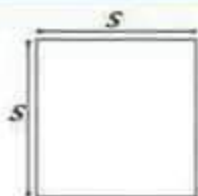
Square	Square Root	Square	Square Root
$1^2 = 1$	$\sqrt{1} = 1$	$16^2 = 256$	$\sqrt{256} = 16$
$2^2 = 4$	$\sqrt{4} = 2$	$17^2 = 289$	$\sqrt{289} = 17$
$3^2 = 9$	$\sqrt{9} = 3$	$18^2 = 324$	$\sqrt{324} = 18$
$4^2 = 16$	$\sqrt{16} = 4$	$19^2 = 361$	$\sqrt{361} = 19$
$5^2 = 25$	$\sqrt{25} = 5$	$20^2 = 400$	$\sqrt{400} = 20$
$6^2 = 36$	$\sqrt{36} = 6$	$21^2 = 441$	$\sqrt{441} = 21$
$7^2 = 49$	$\sqrt{49} = 7$	$22^2 = 484$	$\sqrt{484} = 22$
$8^2 = 64$	$\sqrt{64} = 8$	$23^2 = 529$	$\sqrt{529} = 23$
$9^2 = 81$	$\sqrt{81} = 9$	$24^2 = 576$	$\sqrt{576} = 24$
$10^2 = 100$	$\sqrt{100} = 10$	$25^2 = 625$	$\sqrt{625} = 25$
$11^2 = 121$	$\sqrt{121} = 11$	$26^2 = 676$	$\sqrt{676} = 26$
$12^2 = 144$	$\sqrt{144} = 12$	$27^2 = 729$	$\sqrt{729} = 27$
$13^2 = 169$	$\sqrt{169} = 13$	$28^2 = 784$	$\sqrt{784} = 28$
$14^2 = 196$	$\sqrt{196} = 14$	$29^2 = 841$	$\sqrt{841} = 29$
$15^2 = 225$	$\sqrt{225} = 15$	$30^2 = 900$	$\sqrt{900} = 30$



**SQUARE**

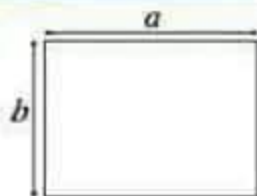
$$P = 4s$$

$$A = s^2$$


**RECTANGLE**

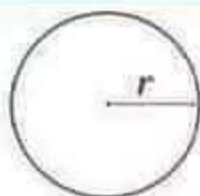
$$P = 2a + 2b$$

$$A = ab$$


**CIRCLE**

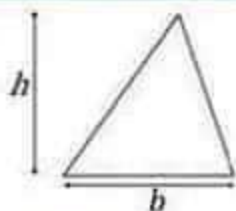
$$P = 2\pi r$$

$$A = \pi r^2$$


**TRIANGLE**

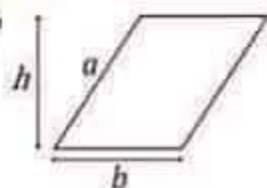
$$P = a + b + c$$

$$A = \frac{1}{2}bh$$


**PARALLELOGRAM**

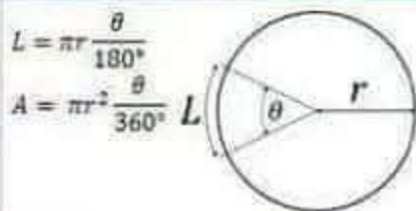
$$P = 2a + 2b$$

$$A = bh$$


**CIRCULAR SECTOR**

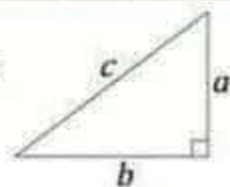
$$L = \pi r \frac{\theta}{180^\circ}$$

$$A = \pi r^2 \frac{\theta}{360^\circ}$$

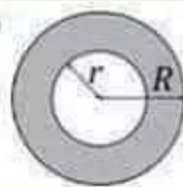

**PYTHAGOREAN THEOREM**

$$a^2 + b^2 = c^2$$

$$c = \sqrt{a^2 + b^2}$$


**CIRCULAR RING**

$$A = \pi(R^2 - r^2)$$


**SPHERE**

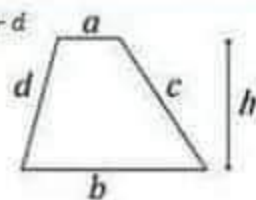
$$S = 4\pi r^2$$

$$V = \frac{4\pi r^3}{3}$$


**TRAPEZOID**

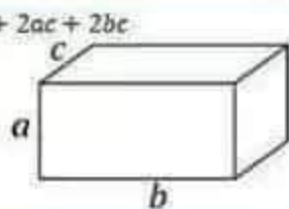
$$P = a + b + c + d$$

$$A = h \frac{a+b}{2}$$


**RECTANGULAR BOX**

$$A = 2ab + 2ac + 2bc$$

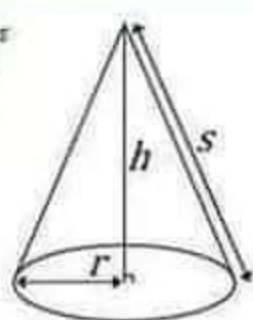
$$V = abc$$


**RIGHT CIRCULAR CONE**

$$A = \pi r^2 + \pi r s$$

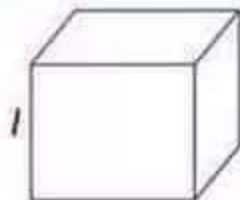
$$s = \sqrt{r^2 + h^2}$$

$$V = \frac{1}{3} \pi r^2 h$$


**CUBE**

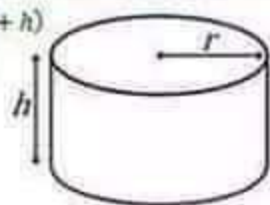
$$A = 6l^2$$

$$V = l^3$$

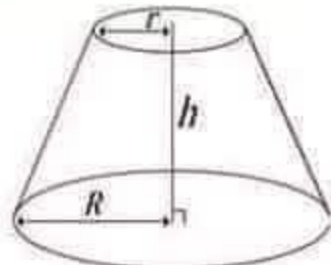

**CYLINDER**

$$A = 2\pi r(r + h)$$

$$V = \pi r^2 h$$


**FRUSTUM OF A CONE**

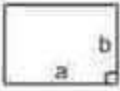
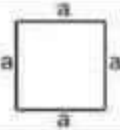

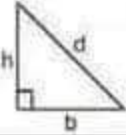

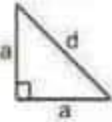
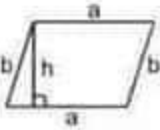
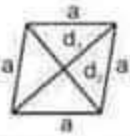


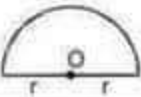


$$V = \frac{1}{3} \pi h (r^2 + rR + R^2)$$



## TRANSITION TO ALGEBRA FORMULA CHART

Distance formula $d = rt$	Percent proportion $\frac{\text{is}}{\text{of}} = \frac{\%}{100}$
Simple Interest formula $I = prt$	Percent of Change $\frac{\text{difference}}{\text{original}} = \frac{\%}{100}$
Distance between to ordered pairs $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$	Midpoint $\left( \frac{x_2 + x_1}{2}, \frac{y_2 + y_1}{2} \right)$
Pythagorean Theorem $c^2 = a^2 + b^2$	Slope of a line $m = \frac{y_2 - y_1}{x_2 - x_1}$
Slope-Intercept Form $y = mx + b$	Perimeter of Square $P = 4s$
Perimeter of Rectangle $P = 2l + 2w$	Volume of Rectangular Prism $V = lwh$
Volume of Cube $V = s^3$	Area of Square $A = s^2$
Area of Rectangle $A = bh$	Area of Triangle $A = \frac{bh}{2}$
Area of Circle $A = \pi r^2$	Area of Trapezoid $A = \frac{1}{2}h(b_1 + b_2)$
Circumference of Circle $C = \pi d$	



Name	Figure	Perimeter	Area
Rectangle		$2(a + b)$	$ab$
Square		$4a$	$a^2$
Triangle		$a + b + c = 2s$	$1 = \frac{1}{2} \times b \times h$ $2 = \frac{1}{s(s-a)(s-b)(s-c)}$
Right triangle		$b + h + d$	$\frac{1}{2}bh$
Equilateral triangle		$3a$	1. $\frac{1}{2}ah$ 2. $\frac{\sqrt{3}}{4}a^2$
Isosceles right triangle		$2a + d$	$\frac{1}{2}a^2$
Parallelogram		$2(a + b)$	$ah$
Rhombus		$4a$	$\frac{1}{2}d_1d_2$
Trapezium		Sum of its four sides	$\frac{1}{2}h(a + b)$
Circle		$2\pi r$	$\pi r^2$
Semicircle		$\pi r + 2r$	$\frac{1}{2}\pi r^2$
Ring (shaded region)		---	$\pi(R^2 - r^2)$
Sector of a circle		$l + 2r$ where $l = \frac{\theta}{360} \times 2\pi r$	$\frac{\theta}{360} \times \pi r^2$

# GEOMETRIC FORMULAS

A = Area P = Perimeter V = Volume

RIGHT TRIANGLE



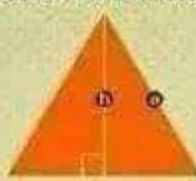
Pythagorean Theorem  $a^2 + b^2 = c^2$

SCALENE TRIANGLE



$A = \frac{1}{2}bh$   $P = a+b+c$

EQUILATERAL TRIANGLE



$A = \frac{\sqrt{3}}{4}a^2$   $h = \frac{\sqrt{3}}{2}a$   $P = 3a$

CIRCLE



$A = \pi r^2$   $P = 2\pi r$

SQUARE



$A = a^2$   $c = \sqrt{2}a$   $P = 4a$

RECTANGLE



$A = ab$   $P = 2a+2b$

TRAPEZOID



$A = \frac{1}{2}(a+b)h$   $P = a+b+c+d$

PARALLELOGRAM



$A = bh$   $P = 2a+2b$

HEXAGON



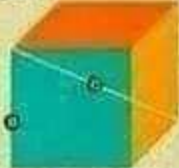
$A = \frac{1}{2}6ar$   $P = 6a$

PENTAGON



$A = \frac{1}{2}5ar$   $P = 5a$

CUBE



$A = 6a^2$   $V = a^3$   $c = \sqrt{3}a$

SPHERE



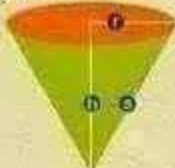
$A = 4\pi r^2$   $V = \frac{4}{3}\pi r^3$

CUBOID



$A = 2ah + 2bh + 2ba$   $V = bah$

CONE



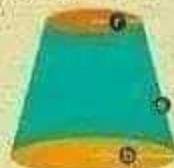
$A = \pi rs + \pi r^2$   $V = \frac{1}{3}\pi r^2 h$

CYLINDER



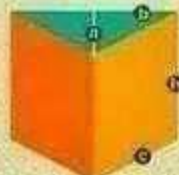
$A = 2\pi r^2 + 2\pi rh$   $V = \pi r^2 h$

FRUSTUM



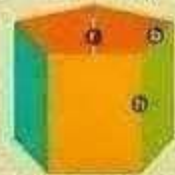
$A = \pi s(b+r) + \pi(b^2 + r^2)$

TRIANGULAR PRISM



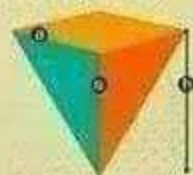
$A = ba + 2hc + hb$   $V = \frac{1}{2}bah$

PENTAGONAL PRISM



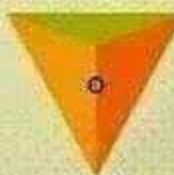
$A = 5rb + 5bh$   $V = \frac{5}{2}rbh$

SQUARE PYRAMID

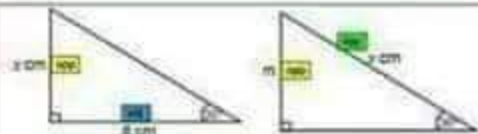


$A = a^2 + 2as$   $V = \frac{1}{3}a^2 h$

TETRAHEDRON



$A = \sqrt{3}a^2$   $V = \frac{a^3}{6\sqrt{3}}$



$$\tan A = \frac{\text{opp}}{\text{adj}}$$

$$\tan 35^\circ = \frac{x}{8}$$

$$8 \times \tan 35^\circ = x$$

$$5.6016603 \times x$$

$$5.6 \text{ cm} = x$$

Finding a side

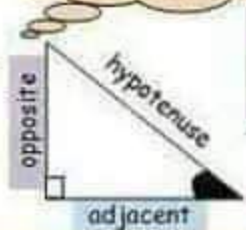
$$\sin A = \frac{\text{opp}}{\text{hyp}}$$

$$\sin 36^\circ = \frac{11}{x}$$

$$x = \frac{11}{\sin 36^\circ}$$

$$x = 18.7 \text{ cm}$$

label the sides of the triangle



$$A^2 + B^2 = C^2$$



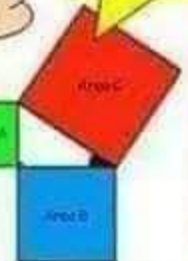
$$x^2 = 9^2 + 7^2$$

$$x^2 = 81 + 49$$

$$x^2 = 130$$

$$x = \sqrt{130} = 11.4$$

Pythagoras' Theorem



hypotenuse - ADD!  
shorter side - SUBTRACT!

# Trigonometry

$$\sin = \frac{\text{opp}}{\text{hyp}}$$

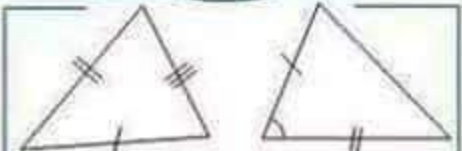
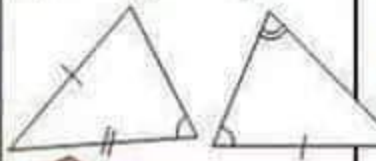
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

sides

## The Sine Rule

$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

angles



$$a^2 = b^2 + c^2 - 2bc \cos A$$

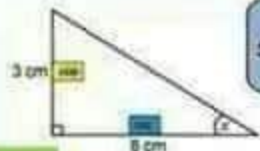
sides

## The Cosine Rule

$$\cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

angles

Finding an angle



$$\tan x = \frac{\text{opp}}{\text{adj}}$$

$$\tan x = \frac{3}{8} = 0.375$$

$$x = \tan^{-1} 0.375$$

$$x = 20.556045$$

$$x = 20.6^\circ$$

$$\cos = \frac{\text{adj}}{\text{hyp}}$$

$$\tan = \frac{\text{opp}}{\text{adj}}$$

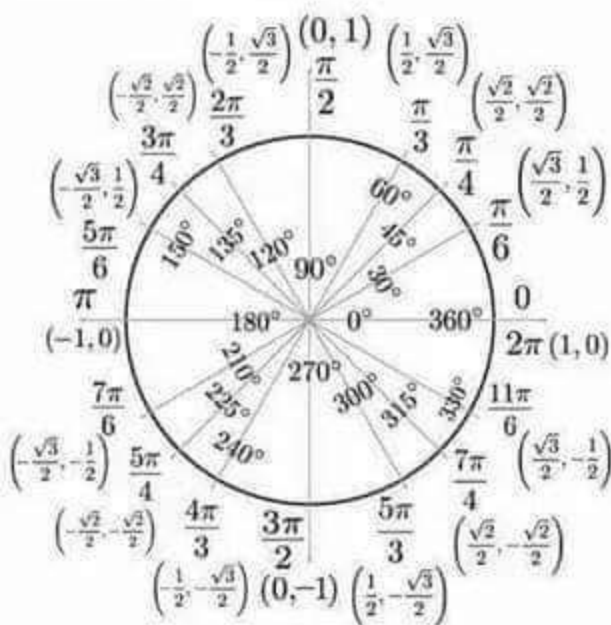
Remember to use the formula page on your exam paper!

$$\text{Area of a triangle} = \frac{1}{2} ab \sin C$$





# Unit Circle



# Unit Circle Table

Degree	cos	sin	tan	sec	csc	cot
$0^\circ$	1	0	0	1	undefined	undefined
$30^\circ$	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$\frac{\sqrt{3}}{3}$	$\frac{2\sqrt{3}}{3}$	2	$\sqrt{3}$
$45^\circ$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{2}}{2}$	1	$\sqrt{2}$	$\sqrt{2}$	1
$60^\circ$	$\frac{1}{2}$	$\frac{\sqrt{3}}{2}$	$\sqrt{3}$	2	$\frac{2\sqrt{3}}{3}$	$\frac{\sqrt{3}}{3}$
$90^\circ$	0	1	undefined	undefined	1	0
$120^\circ$	$-\frac{1}{2}$	$\frac{\sqrt{3}}{2}$	$-\sqrt{3}$	-2	$\frac{2\sqrt{3}}{3}$	$-\frac{\sqrt{3}}{3}$
$135^\circ$	$-\frac{\sqrt{2}}{2}$	$\frac{\sqrt{2}}{2}$	-1	$-\sqrt{2}$	$\sqrt{2}$	-1
$150^\circ$	$-\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$-\frac{\sqrt{3}}{3}$	$-\frac{2\sqrt{3}}{3}$	2	$-\sqrt{3}$
$180^\circ$	-1	0	0	-1	undefined	undefined
$210^\circ$	$-\frac{\sqrt{3}}{2}$	$-\frac{1}{2}$	$\frac{\sqrt{3}}{3}$	$-\frac{2\sqrt{3}}{3}$	-2	$\sqrt{3}$
$225^\circ$	$-\frac{\sqrt{2}}{2}$	$-\frac{\sqrt{2}}{2}$	1	$-\sqrt{2}$	$-\sqrt{2}$	1
$240^\circ$	$-\frac{1}{2}$	$-\frac{\sqrt{3}}{2}$	$\sqrt{3}$	-2	$-\frac{2\sqrt{3}}{3}$	$\frac{\sqrt{3}}{3}$
$270^\circ$	0	-1	undefined	undefined	-1	0
$300^\circ$	$\frac{1}{2}$	$-\frac{\sqrt{3}}{2}$	$-\sqrt{3}$	2	$\frac{2\sqrt{3}}{3}$	$-\frac{\sqrt{3}}{3}$
$315^\circ$	$\frac{\sqrt{2}}{2}$	$-\frac{\sqrt{2}}{2}$	-1	$\sqrt{2}$	$-\sqrt{2}$	-1
$330^\circ$	$\frac{\sqrt{3}}{2}$	$-\frac{1}{2}$	$-\frac{\sqrt{3}}{3}$	$\frac{2\sqrt{3}}{3}$	-2	$-\sqrt{3}$
$360^\circ$	1	0	0	1	undefined	undefined